

9-4 Study Guide and Intervention**Solving Quadratic Equations by Using the Quadratic Formula**

Quadratic Formula To solve the standard form of the quadratic equation, $ax^2 + bx + c = 0$, use the **Quadratic Formula**.

Quadratic Formula	the formula $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ that gives the solutions of $ax^2 + bx + c = 0$, where $a \neq 0$
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Example 1 Solve $x^2 + 2x = 3$ by using the Quadratic Formula.

Rewrite the equation in standard form.

$$\begin{aligned} x^2 + 2x &= 3 && \text{Original equation} \\ x^2 + 2x - 3 &= 3 - 3 && \text{Subtract 3 from each side.} \\ x^2 + 2x - 3 &= 0 && \text{Simplify.} \end{aligned}$$

Now let $a = 1$, $b = 2$, and $c = -3$ in the Quadratic Formula.

$$\begin{aligned} x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\ &= \frac{-2 \pm \sqrt{(2)^2 - 4(1)(-3)}}{2(1)} \\ &= \frac{-2 \pm \sqrt{16}}{2} \\ x &= \frac{-2 + 4}{2} \quad \text{or} \quad x = \frac{-2 - 4}{2} \\ &= 1 \qquad \qquad \qquad = -3 \end{aligned}$$

The solution set is $\{-3, 1\}$.

Example 2 Solve $x^2 - 6x - 2 = 0$ by using the Quadratic Formula. Round to the nearest tenth if necessary.

For this equation $a = 1$, $b = -6$, and $c = -2$.

$$\begin{aligned} x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\ &= \frac{6 \pm \sqrt{(-6)^2 - 4(1)(-2)}}{2(1)} \\ &= \frac{6 \pm \sqrt{44}}{2} \\ x &= \frac{6 + \sqrt{44}}{2} \quad \text{or} \quad x = \frac{6 - \sqrt{44}}{2} \\ &\approx 6.3 \qquad \qquad \qquad \approx -0.3 \end{aligned}$$

The solution set is $\{-0.3, 6.3\}$.

Exercises

Solve each equation by using the Quadratic Formula. Round to the nearest tenth if necessary.

1. $x^2 - 3x + 2 = 0$

2. $m^2 - 8m = -16$

3. $16r^2 - 8r = -1$

4. $x^2 + 5x = 6$

5. $3x^2 + 2x = 8$

6. $8x^2 - 8x - 5 = 0$

7. $-4c^2 + 19c = 21$

8. $2p^2 + 6p = 5$

9. $48x^2 + 22x - 15 = 0$

10. $8x^2 - 4x = 24$

11. $2p^2 + 5p = 8$

12. $8y^2 + 9y - 4 = 0$

13. $2x^2 + 9x + 4 = 0$

14. $8y^2 + 17y + 2 = 0$

15. $3z^2 + 5z - 2 = 0$

16. $-2x^2 + 8x + 4 = 0$

17. $a^2 + 3a = 2$

18. $2y^2 - 6y + 4 = 0$